

# Online wavelets transform on a Xilinx FPGA Circuit to medical images compression

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## ABSTRACT

Knowing that, the computing process of the S. Mallat Transform algorithm is characterized by a purely sequential structure, and from the fact, the on line mode arithmetic is more suitable for the computation of this kind of operations. We propose in this paper, a new wavelet Transform algorithm and a suitable architecture implemented on a Xilinx FPGA circuit. In this study, we will show how on line arithmetic is used to implement a pipelined architecture of the S. Mallat Transform and we will demonstrate through different implementations under different medical image and different computation mode that it might be used successfully for medical image compression.

**Keywords :** Component; Wavelet Transform; On Line Arithmetic; Compression; FPGA Implementation

## I. INTRODUCTION

The wavelet transform is a device used for the decomposition and reconstruction of sign. The multi decision evaluation Mallat's algorithm [1] includes splitting an input signal into subsequent orthogonal indicators containing a filtered version of the enter, the primary split represents the low skip facts, whereas the second represents the high pass facts, each of the output signals is considered to contain discriminate information and may be dealt with one by one in a comparable decomposition [2].

The decomposition conserves the info and approximations corresponding to the excessive and occasional pass outputs at exceptional stages, which lets in a really perfect reconstruction of the unique signal, this approach is specifically utilized in records compression, transmission via slim statistics channels then decompression.

The sequential nature of S.Mallat algorithm constitutes a constraint which reduces sensitively the application subject of the wavelets mainly in the discipline requiring a real time transmission and on excessive speed.

one of a kind packages require information to be available at excessive speed, just like the bit transmission or bit processing whilst related to different levels of a pipeline, to be able to be green on the bit level, the implementation must have optimized records paths.

To remedy to this constraint we endorse using on line mathematics and pipe line structure with a level bit within the execution of the S.Mallat's set of rules.

From this point of view, the online calculation mode could be very efficient, due to the move of the operands in a serial mode, maximum enormous bit (MSB) first. The possibility of having a pipeline on the bit stage makes it viable to have a massive calculation with a tolerable accuracy.

On this have a look at, the primary part concerns some quick statistics approximately the wavelet concept, using the Mallat set of rules, the second section describes a version of the web arithmetic wavelet rework, then at ultimate, we gift an structure for picture on line

arithmetic decomposition an reconstruction is provided and the concluding part deals with the performances.

## II. REVIEW OF S.MALLAT ALGORITHM

The time frequency decomposition of a sign is honestly a filtering of its low and high bypass components, referred to as L and H decompositions, whilst operating with pix a 2nd step of splitting is essential to obtain the LL, LH, HH and HL decompositions [3].

### A. Decomposition / Reconstruction:

The discern shown underneath shows the method of decomposition in the Approximation known as L and information referred to as H; The L branch is the chosen architecture to be carried out at the beginning; this attention is taken, due to the massive quantity of statistics that is within the L bands.

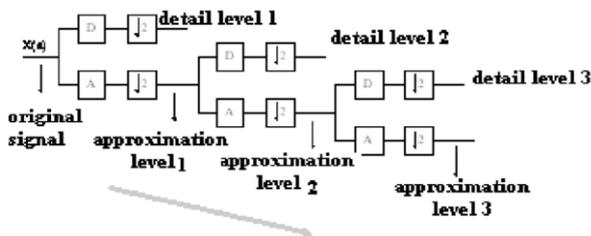


Figure 1. Decomposition scheme Mallat's algorithm

The very last output at every double filtering, either Low Low, Low high, excessive Low, or excessive high convolutions are obtained in the following series:

- Convolve the preliminary photograph in a horizontal zigzag way from the point placed at excessive leftmost role to low rightmost role, with each low and excessive skip filters in parallel, to become with two intermediary pics called L and H of size  $N \times N$ .
- Down sample the photograph from  $N \times N$  points to gain  $N/2 \times N$  factors.
- Convolve the intermediate pics in a vertical zigzag way from the point located at excessive leftmost role to low rightmost position, with both low and excessive skip filters in parallel, to come to be with 4 final photographs referred to as LL, LH, HL and HH.
- Down pattern the photograph from  $N/2 \times N$  factors to end up with  $N/2 \times N/2$  factors.
- The discrete wavelet transform gives us, on the cease of the primary decomposition, a compressed photograph with a component of four.

The reconstruction is the inverse procedure, having in hand the reconstructing filters and the 4 filtered images. (LL, LH, HL, HH). [2].

LL and LH are convolved, up sampled, summed to shape the L department, HL and HH are convolved, up sampled, summed to shape the H branch, the technique is repeated to the L and H branches to turn out to be with the original picture.

The filters used for decomposition and reconstruction are squaring reflect filters to make certain an excellent reconstruction of the associated -channel filter out banks scheme. [4], [5]

## III. EVALUATION OF THE S.MALLAT ALGORITHM BY THE ON LINE MODE

### A. Review of The on line Mode:

In 1961, Avizienis [6] delivered the writing of the numbers in a redundant machine of representation. Later, algorithms of calculation of fundamental operations and greater complex capabilities were elaborated. those algorithms are based at the stream of operands in a piece by means of bit manner, most enormous bit (MSB) first [8], [9].

### B. Mathematical Modelling of S.Mallet algorithm:

The wavelet clear out model is considered to be more than one finite impulse filters FIR of order N, such that:

$$Y_n = \sum_{i=0}^N h_i X_{n-i} \quad (1)$$

$Y_n$ : Output sign ;

$X_n$ : input signal

$h_i$ : Coefficients of the filter

N: is the order of the filter out, it could be exclusive for every of the used filters.

The mathematical improvement is comparable for each high and coffee skip a clear out this is why we keep in mind in our online equations a FIR filter, without a bandwidth obstacle. The online enter output equations given at every step j are defined through:

$$X_n[j] = X_n[j-1] + x_n[j]b^{-j} \quad (2)$$

$$Y_n[j] = Y_n[j-1] + y_n[j]b^{-j} \quad (3)$$

where  $b$  is the premise set to two, for comfort of implementation. The brand new filter out expression is given by way of  $Y_n[j]$

$$= \sum_{i=0}^N h_i X_{n-i}[j] \quad (4)$$

on the  $j$ th step, the result bit  $Y_n^*[j]$  is generated with a bounded mistakes  $\epsilon_j$ , that is defined as comply with:

$$|Y_n^*[j] - Y_n[j]| \leq \epsilon_j \quad (5)$$

Where  $Y_n[j]$  is an appropriate cost and

$$\epsilon_j = \frac{2^{-j}}{2} \quad (5.a)$$

The set of rules does now not compute immediately the actual fee of  $Y_n[j]$ , but a shifted cost  $Y_n^*[j]$  with  $p$  bits shift, proven as beneath:

The price of  $p$  is the put off and may be computed in the next section.

$$Y_n^*[j] = 2^{-p} Y_n[j] \quad (6)$$

From the equations (four), (5) and (6) we reap

$$|2^{-p} Y_n[j] - Y_n^*[j]| \leq \frac{2^{-j}}{2}$$

that is equal to:

$$2^{-p} \left( \sum_{i=0}^N h_i X_{n-i}[j] \right) - Y_n^*[j] \leq \frac{2^{-j}}{2} \quad (7)$$

### C. The partial residue

We outline the partial residue  $R[j]$  as:

$$R[j] = 2^j [2^{-p} \left( \sum_{i=0}^N h_i X_{n-i}[j] \right) - Y_n^*[j]] \quad (8)$$

The set of rules converges if and handiest if:

$$2^{-j} |R[j]| \leq \frac{2^{-j}}{2}$$

This have to be maintained, at a bounded value to make sure convergence at each new release. changing equations, (2) and a not on time version of (three), we reap the following end result:

$$R[j] = 2^j [2^{-p} \left( \sum_{i=0}^N h_i X_{n-i}[j-1] \right) - Y_n^*[j-1]] + 2^{-p} \left( \sum_{i=0}^N h_i X_{n-i}[j] \right) - y_n[j]$$

The recursive expression of  $R[j]$  is simplified to:

$$R[j] = 2 R[j-1] + L[j] - y_n[j] \quad (10)$$

and :

$$L[j] = 2^{-p} \left( \sum_{i=0}^N h_i X_{n-i}[j] \right) \quad (10.a)$$

### D. The entire residue

The complete residue is described by using:

$$H[j] = R[j] + y_n[j] \quad (11)$$

From the equations (10) and (11):

$$H[j] = 2H[j-1] + L[j] - 2y_n[j-1] \quad (12)$$

From the relation in equation (9):

$$-1/2 \leq R[j-1] \leq 1/2 \quad (12.a)$$

the usage of (12.a) and (11)

$$-1/2 + y_n[j] \leq H[j-1] \leq 1/2 + y_n[j] \quad (13)$$

With  $y_n[j] \in \{-1, 0, +1\}$ : most redundancy is used finally, the whole residue defines the cost of the end result bit by the inequality:

$$-3/2 \leq H[j-1] \leq 3/2 \quad (14)$$

From the equations (11) and (12) the choice function is given by  $S(H[j])$  with :

$$\begin{cases} H[j] = 2H[j-1] + L[j] - 2y_n[j-1] \\ y_n[j] = S(H[j]) \end{cases} \quad (15)$$

From the relation in equation (10.a) and (12)

$$L_p[j] = 2^{-p} \sum_{i=0}^N h_i x_{n-i}[j] - 2y_n[j-1] \quad (16)$$

### E. The put off computation:

As said earlier than, one of the bottlenecks of the online mathematics is the delay p, that is defined as how many “bits” will we inject into the equations, for you to attain a chunk end result.

From equations (15), and (10.a)

$$H[j] = 2H[j-1] + L[j] - 2y_n[j-1]$$

$$H[j] = 2H[j-1] + L[j] - 2y[j-1] \quad n \leq 3/2$$

$$\Leftrightarrow p \geq 1 + \log_2(\max(\sum_{i=0}^n h_i x_{n-i}[j]))$$

so that it will enforce the on line architecture with minimal assets, symmetric wavelet coefficients are used. In our look at, we have used the LeGall clear out (are proven desk 1), this one is used for lossless compression and reconstruction inside the JPEG2000 norm. table 1

Considered one of the selection elements of the Le Gall filter is that its coefficients could be modeled as left to right shifts in an implementation point of view [12].to be able to lessen the nonzero wavelet coefficients corresponded to an edge, smaller wide variety of wavelet faucets is extra preferred [13], [14].

	Decomposition	Reconstruction
0	$-1/8=2^{-3}$	$-1/2=2^{-1}$
1	$2/8=2^{-2}$	1
2	$6/8=2^{-3}+2^{-2}$	$-1/2=2^{-1}$
3	$2/8=2^{-2}$	
4	$-1/8=2^{-3}$	

The precision on the coefficients has to be taken into consideration from two elements, the quantification error within the filtering process and the records direction size growth, the Le Gall filter is considered as a fixed of shifts coded in a hard and fast duration check in.

## IV. THE ON LINE S. MALLAT ALGORITHM IMPLEMENTATION

The coronary heart of the implementation is to version the equations of (15).The overall structure of the online S.MALLAT algorithm implementation will be divided into parts as follows:

- Memory bloc or lookup tables for the storage of the pre-computed values of  $L_p(j)$
- The online block for the bit technology from the selection function.

### A. H[j] computation:

$H[j-1]$  is computed thru a adder then multiplied by means of two or honestly shifted; The result is pushed again to the adder and three bits of  $H[j]$  are utilized by the choice circuit to give up the bit result at every generation j [8].

The  $H[j]$  loop is one of the primary bottlenecks of the implementation, because of the time period “upload then loop”, this can wider the data path, this is why, we used the method of [15] to sure the range of bits of  $H[j]$  through computing the duration of this check in.

From [14]

$$w = N + \log_2(m) \quad (17)$$

in which: m= Number of loops =8, It depends of the image type (8 for Gray scale)

$N$ =Operand length =10(8 for the image pixel + 2 bits for the delay)  $w = 8 + \log_2(12) \approx 12$  which is also the length of  $L_p[j]$ , because it represents the second input of the adder as shown in figure 2.

## V. THE GLOBAL ARCHITECTURE

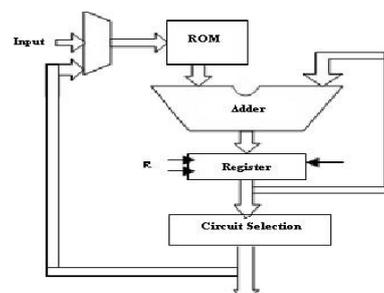


Figure 2. A. Comparative Study Between the Classical and The Proposed Approach

Which will examine, the wide variety of computations performed in a wavelet rework, we took an photo of length 256, and LeGall filter; this can be prolonged to a widespread shape.

Table 2:Order of computations

	Usual method	The proposed approach
Convolutions Number	$(256 \times 256) \times 5 \times 2+$ $(128 \times 256) \times 4 = 786432$	$2 \times (128 \times 128) \times 5 + 128 \times 128 \times 4 = 229376$
Multiplication	3932160	1146880
Addition	3145728	917504

The whole decomposition structure coping with online wavelet remodel is shown in following figure4:

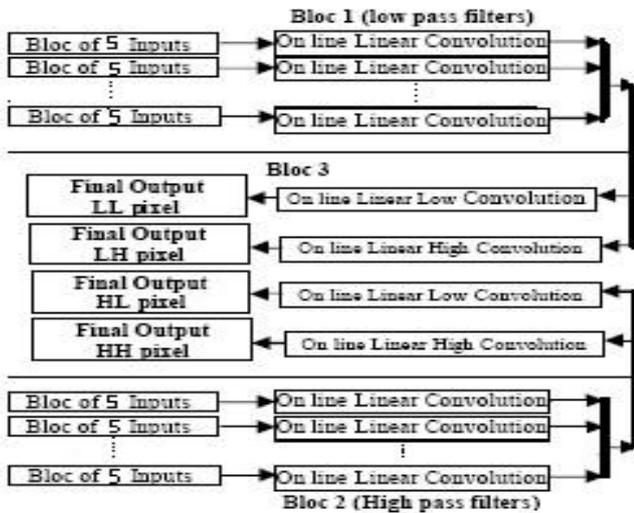


Figure 4. The decomposition matrix wavelet on line block diagram.

In a feasibility method, we examined the proposed on line algorithm beneath Matlab; unique clinical photos has been used as check points and confirmed excellent outcomes; medical photo is shown subsequent, decomposed in the 4 sub bands the use of our architecture simulated below Modeling.

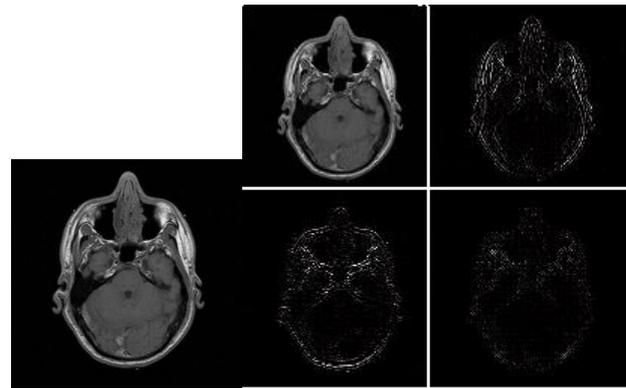


Figure 5. On the left, initial image [15]; on the right the 4 sub bands LL,LH, HL and HH from left to right

### B. Reconstruction degree:

The reconstruction is the reverse technique of the decomposition, based on the obtained sub bands. From each of the 4 sub bands LL, LH, HL, and HH, 4 input pixels are read, leading to 16 online convolutions in parallel.

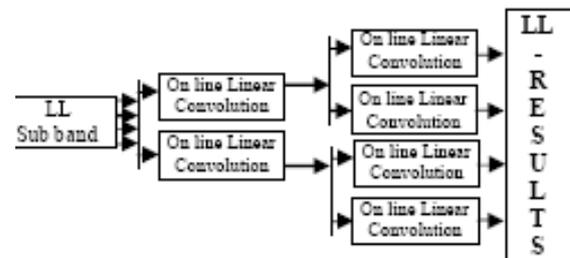


Figure 6. LL sub band Reconstruction architecture

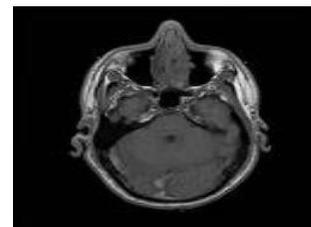


Figure 7. Reconstruction results from the original image under Modelsim

## VI. HARDWARE "SIMULATION" TIMINGS

These timings are software program effects from the Xilinx VirtexII XC2V1000 FPGA, and the overall computation time, each methods used a Pentium IV 2.7 GHz, 512MB of RAM

Table 3. Occuped space from decomposition

Number of Slices:	2191 out of 3072 71%
Number of Slice Flip Flops	189 out of 6144 3%
Number of 4 input LUTs	4143 out of 6144 67%
Number of bonded IOBs	61 out of 172 35%
Number of GCLKs:	1 out of 16 6%

Table 4: Occupied space from reconstruction

Decomposition	51 Mhz
Reconstruction	36 Mhz

Table 5. Obtained Frequencies

Number of Slices:	3278 out of 5120 64%
Number of Slice Flip Flops:	550 out of 10240 5%
Number of 4 input LUTs:	6363 out of 10240 62%
Number of bonded IOBs:	84 out of 328 25%
Number of GCLKs:	1 out of 16 6%

## VII. DISCUSSIONS AND CONCLUSION

In this paper, we've got evolved a new microarchitecture the use of the wave arithmetic for S. Mallat algorithm implementation based totally on the clear out LEGALL five/3 used in the JPEG 2000 trendy for the scientific photographs compression.

The acceleration constraint of coding related to the sequential man or woman of S.Mallat algorithm has been surmounted because of using on-line calculation mode on the one hand and the belief of a pipe line on the extent bit however.

Further the modify microarchitecture allowed the removal of the transient intermediate recollections at some point of the convolutions operations for that reason, the effects received represent a projection inside the answer of two crucial troubles encountered in fashionable JPEG 2000 which might be the acceleration of coding and the reminiscence management.

The implementation at the FPGA of Xilinx Vitrex XC 2V1000 and the tests on samples consultant of clinical pictures made it feasible to reach appreciable performances.

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