A Scheme for Secure Transmission of Multiple Images using MCKBA and FFWPDM

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ABSTRACT

Chaos based encryption may offer new quality in secure data transmission. A recently proposed chaotic-key based algorithm(CKBA) has been shown to be unavoidably susceptible to chosen/known-plaintext attacks and ciphertext-only attacks. In this paper , a new algorithm based on modified chaotic-key based algorithm (MCKBA) and finite field wavelet packet division multiplexing (FFWPDM) is proposed for secure orthogonal multiplexing of images .

Keywords: chaos, cryptography, image encryption, image decryption, wavelet packet division multiplexing

I. INTRODUCTION

The advances in communication technology have seen strong interest in digital signal transmission. However, illegal data access has become more easy and prevalent in wireless and general communication networks. Because of their sensitivity to initial conditions and control parameters, chaotic signals have been used in data encryption [1-5].

In the new chaotic key-based algorithm (CKBA)[1], according to a binary sequence generated from a chaotic system, the gray level of each pixel is XORed or XNORed bit-by-bit to one of the two predetermined keys. The CKBA is simple and attractive with the decryption procedure just like encryption. However, it is proved in [6] that the CKBA is very weak to the chosen/known plain text attack when the same key is used to encrypt more than one image. Further, an improvement to CKBA based on increasing the key sizes is proposed in [6], this only improves the resistance to a cipher text attack only and does nothing to prevent known/chosen plain text attacks. Based on the increased key sizes and piecewise linear chaotic map, an algorithm is reported in [5] to enhance CKBA. A modified chaotic key based algorithm (MCKBA) with increased key size is developed in [7] for improved security. And a new algorithm based on chaos and Brahmagupta–Bhãskara

(BB) equation is developed in [8] for image encryption and decryption with moderate size of keys.

Wavelet packet-division multiplexing (WPDM) is a high-capacity, flexible, and robust multiple-signal transmission technique in which the properties of wavelet packet basis functions are used for orthogonal multiplexing. Finite field wavelet packet-division multiplexing (FFWPDM) provides orthogonal multiplexing of the images and encrypt the images. Finite field Wavelet packet-division multiplexing convert the input images data to a sequence similar to white noise. Hence in this paper a new algorithm is proposed for secure transmultiplexer for images using MCKBA and finite field wavelet packet-division multiplexing (FFWPDM).

II. METHODS AND MATERIAL

2.1 Finite Field Discrete Wavelet Transform

The wavelet system can be implemented using a two-band analysis-synthesis filter bank. Fig. 1 shows the analysis and synthesis banks of a two-channel perfect reconstruction filter bank. More specifically, the analysis bank performs the wavelet transform and the synthesis bank performs the inverse wavelet transform. $X(n)$ is the input data and the sequences labeled $y_0(n)$, $y_1(n)$ are the wavelet coefficients.

Let $H_s(z)$, $G_s(z)$ where $s = 0,1$, be the polynomial representation of the filters $h_s(n)$, $g_s(n)$ in Fig. 1. Suppose that these polynomials have order $2N+1$ with poly phase components $E_{s0}(z)$, $E_{s1}(z)$, $R_{0s}(z)$ and $R_{1s}(z)$ so that

$$H_s(z) = E_{s0}(z^2) + z^{-1}E_{s1}(z^2) \qquad (1)$$

$$G_s(z) = z^{-1}R_{0s}(z^2) + R_{1s}(z^2) \qquad (2)$$

Using the poly phase representation for the two-band orthogonal filter banks, the following can be deduced:

$$H_1(z) = -z^{-(2N+1)}H_0(-z^{-1}) \; ,$$

$$G_0(z) = H_1(-z) \; , \quad G_1(z) = -H_0(-z) \qquad (3)$$

Any two polynomials $A(Z)$ and $B(Z)$ over a Galois field $F(Z)$ that satisfy the polynomial equation

$$A(z)A^c(z) + B(z)B^c(z) = Z^M \qquad (4)$$

can be used to generate the coefficients of wavelet filter banks. The polynomials $A(Z)$ and $B(Z)$ over a Galois field $F(Z)$ are defined as

$$A(z) = \sum_{i=0}^{M} a_i z^i, \ a_0 \neq 0, \quad B(z) = \sum_{i=0}^{M} b_i z^i, \ b_k \neq 0, \qquad (5)$$

$$a_i, b_i \in GF(p^r)$$

where M is a positive integer satisfying M<=N

In our notation, the superscript "c" means the reciprocal of the polynomial. The reciprocal of a polynomial $q(z)$ of degree M is defined as $q^c(z) = z^M q(z^{-1})$

The coefficients of the two polynomials $A(Z)$ and $B(z)$ are related to the poly phase components $E_{00}(z)$ and $E_{01}(z)$ by

$$E_{00}(z) = A(z^{-1}) \quad , \quad E_{01}(z) = z^{M-N}B(z^{-1}) \qquad (6)$$

The M channel transmultiplexer is shown fig. 2a. Finite field two-band orthogonal filter banks are used to construct a finite field wavelet packet-division multiplexing (FFWPDM) transmultiplexer for four-users which is shown fig 2b.

2.2 The Proposed Secure Transmultiplexer Algorithms Based on Chaos and FFWPDM

The chaotic function that used is the well-known logistic map given by

$$x(i+1) = \mu x(i)(1-x(i)) \qquad (7)$$

where $\mu = 3.9$. Let g denote an image of size MxN pixels and f(x, y), $0 \leq x \leq M-1, 0 \leq y \leq N-1$, be the gray level f at position (x, y).

A. The Proposed MCKBA -FFWPDM for multiplexer

The MCKBA for encryption is as follows.

Step 1: choose key1 and key2 and set j=0

Step 2: Choose the initial point x(0) and generate the chaotic sequence x(0), x(1), x(2),…., x(MN/16-1) using eq.(1) and then create b(0), b(1), b(2), …., b(2MN-1) from x(0), x(1),x(2),….., x(MN/16 -1) by the generating scheme such that b(32i+0) b(32i+1)… b(32i+29) b (32i+30) b(32i+31)… is the binary representation of x (i) for i = 0, 1, 2,.. ..(MN/16-1).

Step 3: For x=0 to M-1

    For y = 0 to N-1

    Switch (2×b(j) + b (j+1))

      Case 3: $f_e(x, y) = \mathrm{mod}((f(x, y)+key1), 2^{n-1})$

        $f_e(x, y) = f_e(x, y)$ XOR key1

      Case 2: $f_e(x, y) = \mathrm{mod}((f(x, y)+key1), 2^{n-1})$

        $f_e(x, y) = f_e(x, y)$ XNOR key1

      Case 1: $f_e(x, y) = \mathrm{mod}((f(x, y)+key2), 2^{n-1})$

        $f_e(x, y) = f_e(x, y)$ XOR key2

      Case 0: $f_e(x, y) = \mathrm{mod}((f(x, y)+key2), 2^{n-1})$

        $f_e(x ,y) = f_e(x, y)$ XNOR key2

      = j+2;

      End; End

Step 4: apply the above steps for images f_1, f_2, f_3 and f_4 and obtain f_{e1}, f_{e2}, f_{e3} and f_{e4}.

Step 5: apply the f_{e1}, f_{e2}, f_{e3} and f_{e4} to FFWPDM multiplexer to obtain F .

B. The Proposed MCKBA -FFWPDM for demultiplexer

Step 1: apply the F to FFWPDM demultiplexer to obtain f_{e1}, f_{e2}, f_{e3} and f_{e4}.

Step 2: choose key1 and key2 and set j=0

Step 3: Choose the initial point x(0) and generate the chaotic sequence x(0), x(1), x(2),…., x(MN/16-1) using eq.(1) and then create b(0), b(1), b(2), …., b(2MN-1) from x(0), x(1), x(2),….., x(MN/16 -1) by the generating scheme such that b(32i+0) b(32i+1)… b(32i+29) b(32i+30) b(32i+31)… is the binary representation of x(i) for i = 0, 1, 2,.. ..(MN/16-1)

Step 4:   For x=0 to M-1

     For y = 0 to N-1

     Switch (2×b(j) + b(j+1))

     case 3: f(x,y) = f_e(x,y)XOR key1

          f(x,y) = mod((f(x,y)-key1),2^{n-1})

     case 2: f(x,y) = f_e(x,y)XNOR key1

          f(x,y)= mod((f(x,y)-key1),2^{n-1})

     case 1: f(x,y) = f_e(x,y) XOR key2

          f(x,y) = mod((f(x,y)-key2),2^{n-1})

     case 0: f(x,y) = f_e(x,y)XNOR key2

          f(x,y) = mod((f(x,y)-key2),2^{n-1})

     j= j+2;

     End; End

Step 5: Apply the above steps 2 to 4 for images f_{e1}, fe2, fe3 and f_{e4} to obtain f_1,f_2, f_3 and f_4.

The 'mod' stands for modulus after division.

Because not all secrete keys can make well disorderly encrypted images, the basic criterion to select key1and key2 should satisfy $\sum_{i=0}^{n-1}$ ($a_i \oplus d_i$) = n/2,

key1 = $\sum_{i=0}^{n-1} a_i \times 2^i$ and key2 = $\sum_{i=0}^{n-1} d_i \times 2^i$, n is bit length of key1 and key2

III. RESULTS AND DISCUSSION

SIMULATION RESULTS

The secure transmultiplexer for four users is implemented using MCKBA -FFWPDM on the 8 bits per pixel 256X256 Girl(LENA),Cameraman, goldenear and IC images in GF(2^{18}). The original Girl(LENA),Cameraman, goldenear and IC images are shown in Fig. 8(a). In the implementation of secure transmultiplexer using MCKBA -FFWPDM, 16 bit keys

are used. The key1 and key2 are set to key1 = 36408 (1000111000111000_2) and key2 = 61499 (1111000000111011_2) and $\mu = 3.9$, x (0) =0.75, are used for the logistic maps. The floating point arithmetic is used for logistic map. The filter banks are constructed over GF (2^{18}) with the primitive polynomial $q(x) = x^{18} + x^7 + 1$. The polynomials and $B(z) = 131014 + z$ are used. The corresponding poly phase components are $E_{00}(z) = 131009 + 7z^{-1}$, $E_{01}(z) = 131014 + z^{-1}$

The multiplexed image obtained using secure transmultiplexer using MCKBA -FFWPDM is shown in Fig. 8(b). From Fig. 8(b), it can be observed that the secure transmultiplexer using MCKBA -FFWPDM has created highly disordered image of the original images. The demultiplexed images using secure transmultiplexer using MCKBA -FFWPDM are same as original images as FFWPDM is lossless transform.
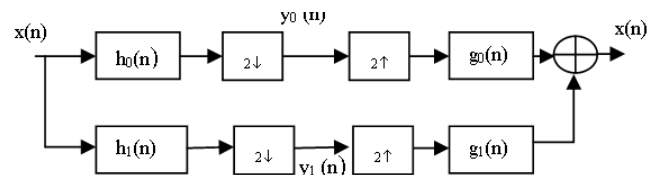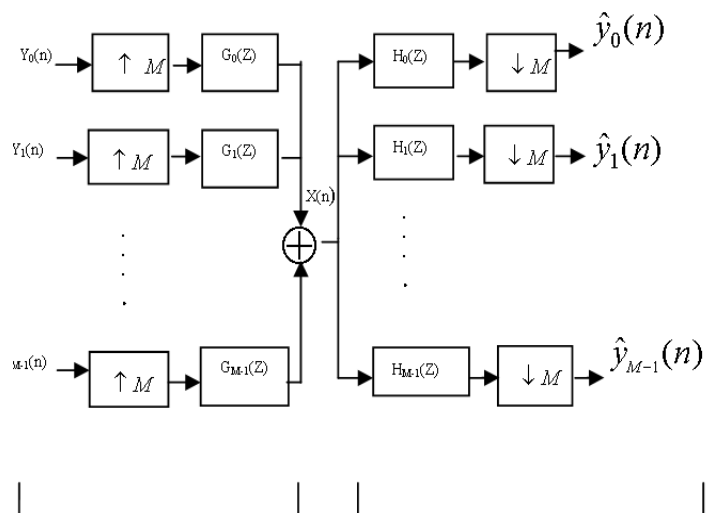

Fig. 1 Two band wavelet filter bank

Fig 2a M channel transmultiplexer Synthesis(Transmitting) Bank   M channel transmultiplexer Analysis(Receiving) Bank
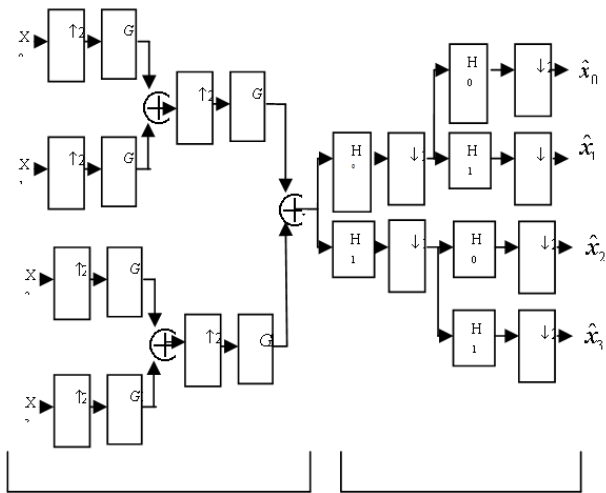
Fig 2b. Four user FFWPDM synthesis bank (Multiplexer)
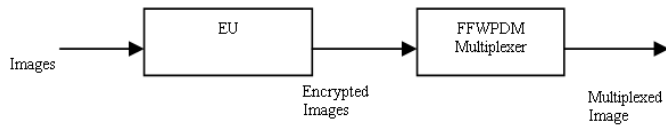
Four user FFWPDM analysis bank (Demultiplexer)
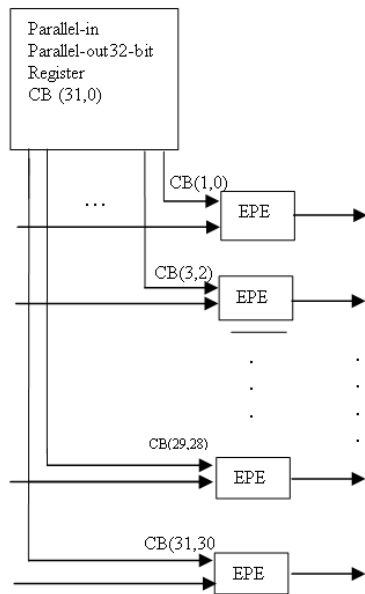

Fig. 3 Cascade architecture of EU and FFWPDM Multiplexer

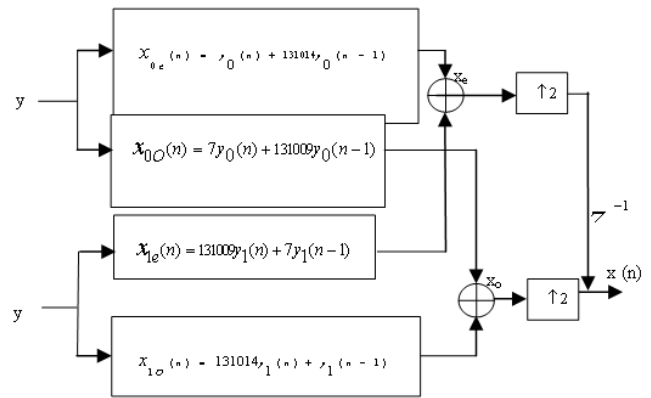Fig.4 Architecture of Encryption Unit

$$x_{0e}(n) = 7y_0(n) + 131014y_0(n-1)$$

$$x_{0O}(n) = 7y_0(n) + 131009y_0(n-1)$$

$$x_{1e}(n) = 131009y_1(n) + 7y_1(n-1)$$

$$x_{1O}(n) = 131014y_1(n) + 7y_1(n-1)$$

Fig. 5 Architecture of FFWPDM synthesis lowpass filter and high pass filter

Fig. 6 Cascade architecture of FFWPDM demultiplexer and DU

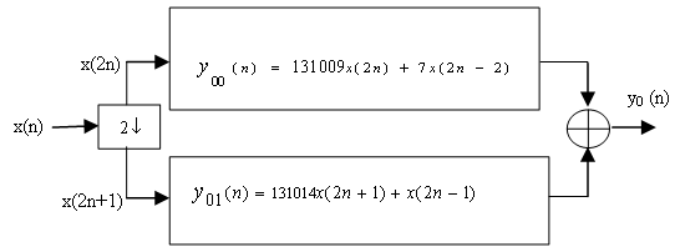$$y_{00}(n) = 131009x(2n) + 7x(2n-2)$$

$$y_{01}(n) = 131014x(2n+1) + x(2n-1)$$

Fig.7 (a) Architecture of FFWPDM analysis low pass filter

$$y_{10}(n) = x(2n) + 131014x(2n-2)$$
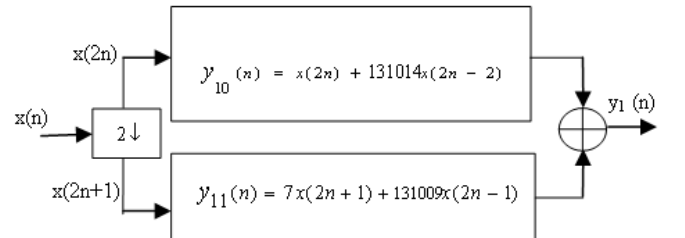
$$y_{11}(n) = 7x(2n+1) + 131009x(2n-1)$$

Fig.7 (b) Architecture of FFWPDM analysis high pass filter
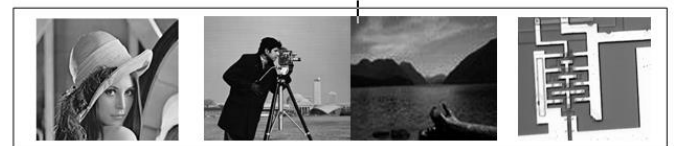

Fig. 8 (a) Original images Lena, cameraman, goldenear and IC

Fig. 8 (b) Multiplexed image using MCKBA-FFWPDM Multiplexer

IV. CONCLUSION

In this paper, a secure transmultiplexer for images using modified chaotic key-Based algorithm and finite field wavelet packet-division multiplexing (MCKBA–FFWPDM) with moderate size of keys is proposed. It gives more security to data.

V. REFERENCES

[1] Jui-cheng Yen and Jiun-In Guo, "A New Chaotic Key –Based Design for Image Encryption and Decryption, ," Proc. IEEE International Symposium on Circuits and Systems, May 28-31, 2000, Geneva, Switzerland, vol. IV, pp.49-52.

[2] N. Masuda . and K. Aihara , "Cryptosystems with discretized chaotic maps," IEEE Trans. on Circuits and Systems - I: Fundamental Theory and Applications, 2002, vol. 49, no. 1, page(s): 28-40.

[3] B. Furht and D. Socek. Multimedia security: encryptiontechniques. In IEC Comprehensive Report on InformationSecurity, International Engineering Consortium,Chicago, IL, pages 335.349, 2004

[4] S. Li, G. Chen, and X. Zheng. Chaos-based encryptionfor digital images and videos, in B. Furht andD. Kirovski (Eds.), Multimedia Security Handbook,Vol. 4 of Internet and Communications Series, Ch. 3,CRC Press, December 2004.

[5] D. Socek, S.Li, S. S. Magliveras, and B. Furht, "Enhanced 1-D Chaotic Key-Based Algorithm for Image Encryption,"Proc. IEEE First International Conference on Security and Privacy for Emerging Areas in Communications Networks, 2005. SecureComm 2005, Sep. 2005.

[6] S. Li and X. Zheng, "Cryptanalysis of a Chaotic Image Encryption Method", ISCAS 2002, vol. 2, pp. 708-711, 2002.

[7] K.Deergha Rao and Ch. Gangadhar, "Modified chaotic key-based algorithm for image encryption and its VLSI realization" IEEE International Conference on Digital Signal Processing (DSP-2007), July 1-4, 2007, Cardiff, Wales, U.K, pp. 439 - 442.

[8] K.Deergha Rao and Ch. Gangadhar, "VLSI Realization of a Secure Cryptosystem for Image Encryption and Decryption" ,IEEE International Conference on Communications and Signal Processing (ICCSP 2011) ,10-12, February 2011,NIT Calicut,Kerala, India.