

A Collision Free Network with Minimal Routing Path for 2^n Nodes

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ABSTRACT

In the present work, a simple but complex network which has collision free communications is created. With the help of the binary n-cube the network is formed. This n-cube network connection is formed by connecting distinct N number of nodes which are expressed as a power of 2. If each node has an address of m bits then there are $N=2^m$ number of nodes in the n-cube network. To find out the predefined routing path for the case of this n-cube network, we can apply deterministic algorithm providing us a collision /deadlock free concept. In calculating the predefined routing path(s), node addresses involved in the path are calculated by using the exclusive OR operation, firstly, upon the two node addresses of source and destination, and then, on the derived node-addresses according to the algorithm stated in section 2. Here, the Exclusive-OR operation is performed simply by using 2-input XOR gate which may be made up of either (i) classical CMOS based material, or (ii) *Multiple input threshold logic gate*, or (iii) Single electron tunneling Transistor (SET). We are concentrated in the case of CMOS based XOR circuit. In this work, an E-cube Routing on a 6-dimensional hypercube has been designed and constructed. We have tried to find out the node addresses for predefining the deadlock free routing path for any set of “source and destination”. To develop a “Collision free network with minimal Routing”, a number of Exclusive-OR gates are arranged in a pattern discussed in section 3 and the desired circuit is implemented. The implemented circuit can supply the predefined path nodes through which the signal/packets/data can pass. Regarding the experimental input –output values, some truth tables are depicted in substantial places. At the time of applying the algorithm, we have investigated that for 6-dimensional hypercube, the maximum path length are confined to 6, i.e. whenever the source and destination points are provided, then 6-node points are produced. Among these 6-points some of them may have identical values. As a result path length should be less than 6. For the network, the time required to travel a path is measured and shown. The net designed and implemented must be a collision free one, since when a truth table is written, there would not be any pair of nodes identical in a column.

Keywords : XOR, Routing-Path, N-Cube, Collision Free, Deadlock, Tree

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I. INTRODUCTION

Packet routing may be conducted either by deterministically or adaptively, in a network. Relying on the network conditions we can prefer the adaptive routing. In the adaptive routing process an alternate path is possible. But for the case of deterministic routing, the routing path from source point to the goal/destination is strictly determined by the starting/source point node address as well as goal/destination node point address. In such case, the routing path must be measured irrespective of network condition in advance. Dimension order routing is the concept emerging from the algorithm of deterministic routing.

Dimension order routing requires to choose the successive channels or sequential node addresses in order to follow a specific order depending on the dimensions of multidimensional network. If we choose the networking in two dimensional mesh, the scheme is called X-Y routing. When we are thinking of a *n* – *cube* network, then the scheme is defined as the E-cube routing [1-5, 12].

Our intention is to make some logical expressions by which we must be able to measure the routing path related nodes so as to travel the routing path through the nodes calculated.

With the help of the tree, the travelling path can be represented. As every nodes contains 6 arms in the network, the tree will be of branch factor = 6. In a full-fledged tree of branch factor 6, there will be $\sum_{i=1}^6 6^i=55986$ nodes where some of nodes are repeated. But for the welfare of the algorithm, only 2-6 nodes are sufficient to go from one node to another. This is the beauty of the algorithm used here. The less the nodes used, the less the time complexity and space complexity will be there.

Routing over a n-dimensional hypercube for 2^n nodes

We think of an n-cube having 2^n nodes (peaks). Every node (p) in n-cube is coded in binary form like $p = p_{n-1}p_{n-2}p_{n-3} \dots p_1p_0$. The source node from which we are interested in starting routing is $s = s_{n-1}s_{n-2}s_{n-3} \dots s_1s_0$. And the destination node to which the routing ends is $d = d_{n-1}d_{n-2}d_{n-3} \dots d_1d_0$. Now we need to find out the destination length from source(s) to destination (d) with the help of a small number of nodes or steps required.

We indicate the n-dimensions in the present situation as $i = 0, 1, 2, 3, \dots, n - 1$; where the i^{th} dimension marks to the $(i - 1)^{\text{th}}$ bit in a node to be represented by $q = q_{n-1}q_{n-2}q_{n-3} \dots q_1q_0$. Suppose q is any node along the route to be gone through. The route from source(s) node to the destination (d) node can be determined by the following algorithm.

Algorithm:

- (i) Measure the direction bit $k_i = s_{i-1} \oplus d_{i-1}$ for all i in n-dimensions i.e. $i = 1, 2, 3, \dots, n$; Commence with dimension $i = 1$ and $q = s$ and follow the following.
- (ii) Start routing from the node q to the next node as $q \oplus 2^{i-1}$ if $k_i = 1$. Skip the step whenever $k_i = 0$.
- (iii) Move to the next dimension $i + 1$, that is $i \leftarrow i + 1$. If $i \leq n$ go to the step (ii), else done.

By taking an example, the algorithm written above can be explained. Consider an E-cube routing over a 6-dimensional hypercube given in Fig. 1.

Here, we have chosen the dimension $n = 6$, so the number of nodes is equal to $2^6=64$, the nodes are represented by 000000, 000001, 000010, ..., 111111. For the case of routing, we assume that the source and destination nodes are S=000100 and D=011100

respectively. So, $k = k_6k_5k_4k_3k_2k_1 = (S \oplus D) = 011000$. We skip the dimension $i = 1, 2, 3$ and 6 as $k_1 = 0 \oplus 0 = 0, k_2 = 0 \oplus 0 = 0, k_3 = 1 \oplus 1 = 0$ and $k_6 = 0 \oplus 0 = 0$ respectively. Now we are to route from source(s) node 000100 to $S \oplus (00k_4000) = 000100 \oplus 01000 = 001100$, since $k_4 = 0 \oplus 1 = 1$. Next route from $q = 001100$ to the to $q \oplus (0k_50000) = 011100$, since $k_5 = 0 \oplus 1 = 1$. As a result, the routing path should be: $000100 \rightarrow 001100 \rightarrow 011100$.

Similarly, If we take another set of inputs, i.e. source and destination like $S=100110$ and $D=001001$ we obtain-

Source = $(s_5s_4s_3s_2s_1s_0) = 100110$

Destination = $(d_5d_4d_3d_2d_1d_0) = 001001$

$k_6 k_5 k_4 k_3 k_2 k_1 = 101111$, in this case $k_5 = 0$

Routing path :

$100110 \rightarrow 100111 \rightarrow 100101 \rightarrow 100001 \rightarrow 101001 \rightarrow$

001001 and this path is shown in the Fig. 1 by thick green lines with arrows.

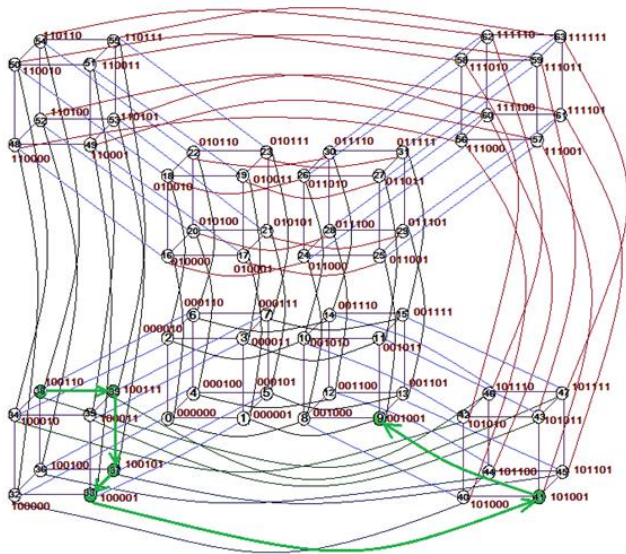


Fig.1 A routing Path with green color from $S=100110$ and $D=001001$

Circuit diagram for creating Path points

The circuit shown in Fig.1 consists of 64 node points and every node has 6 arms (which are bidirectional: incoming or out-going). If a packet is being tried to send from a point to another point, which path it follows is

to be determined earlier otherwise the packet will fall in a labyrinth which is unexpected and undesirable. To overcome this problem, a deterministic path of 6 points will be predicted previously. Such a circuit drawn in Fig. 2 is capable of producing a set of six points, among them some may be identical, by using some identical XOR gates.

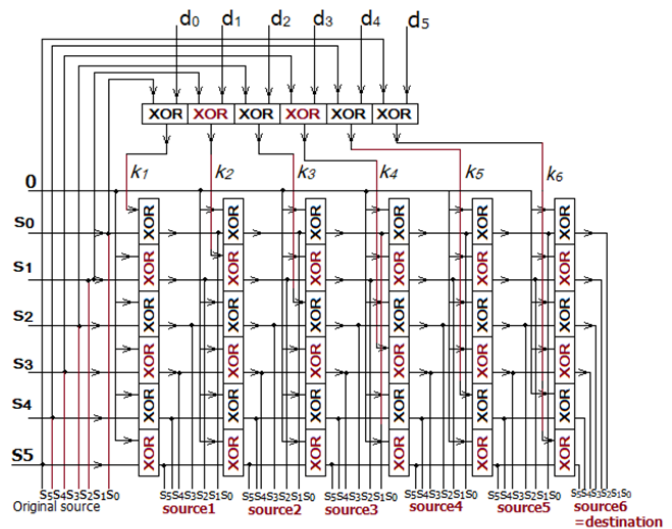


Fig. 2 Block diagram of finding out intermediate nodes of any routing path

According to the diagram drawn in the Fig. 2 as well as the algorithm, we find it easy to get the routing path from source to destination. Some paths consisting of the nodes or vertices of the cube are listed in the Table-1 below. In the diagram above, if we give the source and destination values to input terminals, the output results we got from the output terminals which are given in the Table-1. Depending upon the number of nodes involved in a path, we have calculated the path length. Equation of the path length is given by the following relation:

Path length = number of nodes involved - 1.

For instance, consider the serial number 25 in Table-1. There are 6 non-identical nodes (00000, 00001, 00011, 00111, 01111, 11111) in a routing path, so the $path\ length = 6 - 1 = 5$. Similarly, for serial number 9, there are 4 different nodes (101011, 101010, 101110, 001110) involved in the path, therefore the

$path\ length = 4 - 1 = 3$.

Path number can also be measured as total number of '1' in $k = k_6k_5k_4k_3k_2k_1 = (S \oplus D)$. Consider the 1st row in Table-1, we get $k = k_6k_5k_4k_3k_2k_1 = (110010 \oplus 101101) = 011111$. As there are five 1s in $k = k_6k_5k_4k_3k_2k_1 = 011111$, so the path length is 5.

Note that if somebody look into the Table-1, (s)he will get rarely the same 6-bit words in a column. It is an indication that there will be no confliction in the network in Fig.1 when applied above cited algorithm. In short, there should be no dead lock in the 6-dimensional routing process.

Table-1. Minimum routing path(s)

Sl. No.	Source(s) node number	Destination node number	Source 1 original	Source 2	Source 3	Source 4	Source 5	Source 6	goal	Routing Path Length
1	50	45	110010	110011	110001	110101	111101	101101	101101	5
2	10	18	001010	001010	001010	001010	000010	010010	010010	3
3	0	18	000000	000000	000010	000010	000010	010010	010010	3
4	46	12	101110	101110	101100	101100	101100	101100	001100	2
5	20	30	010100	010100	010110	010110	011110	011110	011110	2
6	39	54	100111	100110	100110	100110	100110	110110	110110	2
7	3	59	000011	000011	000011	000011	001011	011011	111011	3
8	14	61	001110	001111	001101	001101	001101	011101	111101	4
9	43	14	101011	101010	101010	101110	101110	101110	001110	3
10	1	33	000001	000001	000001	000001	000001	000001	100001	1
11	24	36	010110	010110	010100	010100	010100	000100	100100	3
12	20	7	011000	011001	011011	011111	010111	000111	000111	5
13	25	12	011001	011000	011000	011100	011100	001100	001100	3
14	62	5	111110	111111	111101	111101	110101	100101	000101	5
15	7	15	000111	000111	000111	000111	001111	001111	001111	1
16	63	9	111111	111111	111101	111001	111001	101001	001001	4
17	0	22	000000	000000	000010	000110	000110	010110	010110	3
18	55	19	110111	110111	110111	110011	110011	110011	010011	2
19	11	42	001011	001010	001010	001010	001010	001010	101010	3
20	50	60	110010	110010	110000	110100	111100	111100	111100	3
21	2	10	000010	000010	000010	000010	001010	001010	001010	1
22	41	11	101001	101001	101011	101011	101011	101011	001011	2
23	23	7	010111	010111	010111	010111	010111	000111	000111	1
24	6	48	000110	000110	000100	000000	000000	010000	110000	4
25	0	63	000000	000001	000011	000111	001111	011111	111111	6

From the Table -1, it is realizable that the maximal routing path from any set of “(source node, destination node)” is 6. For any set of two non-identical nodes, the routing path length varies from 1 to 6. If we wish to draw a tree for a source node as root node regarding the Table-1 or Fig. 1, we will have a tree of height 6 and branch factor is 6. Below, in Fig. 3(a), Fig. 3(b) and Fig. 3(c) are the three examples which indicate routing path(s) from source/root node(s) to the destination node(s).

Assuming that all 25 sets of (source, destination) are applied at a particular time in Fig.1, then from the Table-1, we will observe that in every row, there are seven words of length 6. But you will not find any two words identical in any column. So there is no probability/chance of conflict/ collision in the network in the Fig.1.

In general, for an n-bit number of a network system will have total number of nodes = 2^n . When we take a node as the source point, there would have $2^n - 1$ destination(s) and travelling the path towards the destination is a more complex job. For searching the goal point from the source point, different searching process can be applied and the respective time and space complexity can be measured. But the algorithm used in this work can determine the different node numbers present in the routing path very easily and it tells us that path length will be no more than n i.e. $1 \leq \text{path length} \leq n$. As we have chosen $n=6$, so $1 \leq \text{path length} \leq 6$. And the time complexity will be limited to $n=6$.

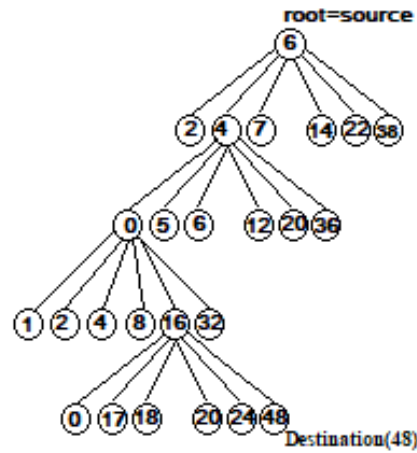


Fig. 3(a) Source to destination length=4

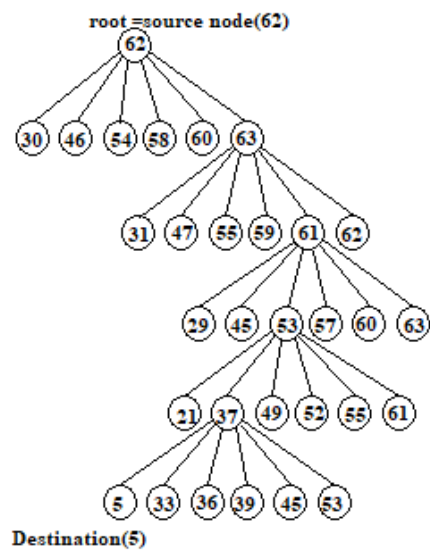


Fig.3(b) Source to destination length=5

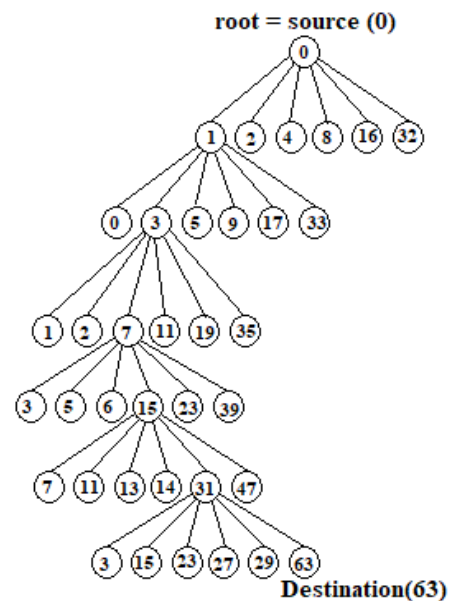


Fig.3(c) Source to destination length=6

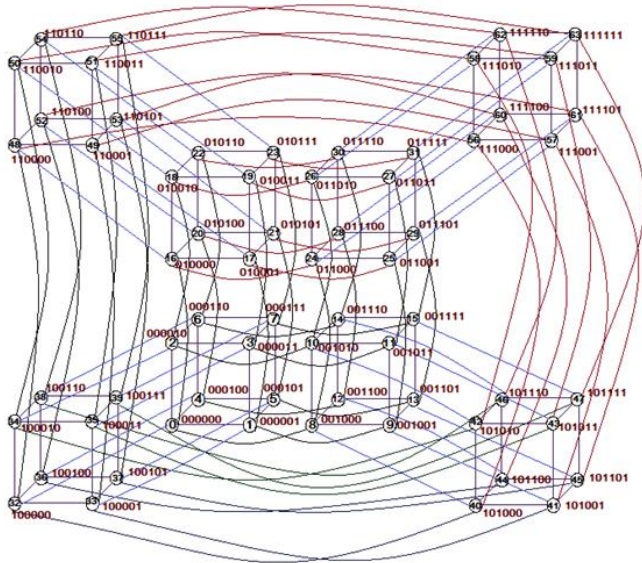


Fig. 4 a network connection of $2^6=64$ nodes starting from 0 to 63

101010 42 _S	101011 43	101110 46	101111 47 _S	111010 58	111011 59	111110 62	111111 63 _D
101000 40	101001 41	101100 44	101101 45	111000 56	111001 57	111100 60	111101 61 _D
100010 34	100011 35	100110 38	100111 39	110010 50	110011 51	110110 54	110111 55
100000 32	100001 33 _D	100100 36	100101 37	110000 48	110001 49	110100 52	110101 53
001010 10	001011 11	001110 14	001111 15 _S	011010 26	011011 27 _D	011110 30	011111 31
001000 8	001001 9 _S	001100 12	001101 13	011000 24	011001 25 _D	011100 28	011101 29
000010 2	000011 3 _S	000110 6	000111 7	010010 18	010011 19	010110 22	010111 23
000000 0	000001 1	000100 4 _S	000101 5	010000 16 _S	010001 17	010100 20	010101 21 _D

Fig.5 Pictorial view of 64 nodes based on gray code and different source to destination nodes with routing paths

For clear understanding, the communication path between two nodes of any set of two numbers (0, 1, 2, ..., 63), a pictorial view of nodes are arranged in 8x8 small squares in Fig. 5. If we want to communicate between any pair of two nodes, we can put the two numbers for the source and destination. The circuit shown in Fig. 2 will provide the communication path showing the nodes connecting the path. A 8x8 node

presentation view is depicted in Fig. 5 and some routing paths for some sources and destinations are marked by arrow lines. For example, two numbers 50 and 27 we have chosen, where 50 is the source and 27 is the goal. As soon as we put these two numbers in the circuit in Fig.2, the outputs from the circuit provide us the numbers 50→51→59→27 with path length 3 and this path is shown in Fig. 5. Similarly, some pairs of nodes are taken arbitrarily and are set in the circuit in Fig.2 as inputs, we get their respective outputs, which are tabulated in the Table-2. According to node arrangement in Fig.3, the travelling direction from one point to the next will be either left or right or above or below, but never diagonally.

Table-2

Sl. No.	Input node	Output node	Routing path	Path length
1	9	33	9→1→33	2
2	16	20	16→20	1
3	15	51	15→11→3→19→51	4
4	48	34	48→34	1
5	16	46	16→20→22→30→14→46	5
6	42	21	42→43→41→45→37→53→21	6
7	50	27	50→51→59→27	3
8	4	63	4→5→7→15→31→63	5
9	34	39	34→35→39	2
10	47	61	47→45→61	2

Collision free/Deadlock free arrangement

According to our algorithm maximum path length =6 when n=6 and the nodes concerned here is 6+1=7. For the worst case, a full-fledged tree having branch factor 6, will be $1+6+6^2+6^3+6^4+6^5+6^6=55986$ nodes where some of nodes are reused in our present work. But for the curtesy of the algorithm, only 2-6 nodes are sufficient to go from one node to another. This is the beauty that the algorithm ensures us a small number of nodes are necessary.

In Table-2 and Table-3, some input–output nodes and the corresponding paths are shown. Unlike Table-2 and Table-3, in Table-1 we have listed all the sequential node points involved in a routing path. If you go through the table, you must feel that no two or more node values are the same in a column. So, at a particular time there will be no chance of collision, therefore it would be a deadlock free arrangement in the network involved here.

Memory size

As the network we are considering has 64 nodes and every node address is of 6 bits. So storing this 6-bits in a memory system at least 1byte memory space is essential. For entire network the memory space required =64byte. Since, in our network, path length for a routing path varies from 1 to 6, the corresponding nodes required would be from 2 to 7. For storing these node addresses bit, the memory size needed will be 2byte to 7byte. In average it is 4.5byte≅5byte. At a time, for travelling a routing path, the memory size manipulated is 7 byte (in worst case). So the memory utilization is $\frac{7}{64} \times 100\% = 10.94\%$, at most.

Delay and speed Calculation

The circuit drawn in Fig. 2 is made up of XOR gates only. Total number of XOR gates is 42. We know the delay for CMOS based XOR gate is 12ns [9, 10], for SET (single electron tunneling transistor) based circuit it is 4ns[8] and for linear threshold logic gate (TLG) based circuit is 2.21ns [5-7]. The communicating delay between two direct connected node points varies and depends upon the communicated materials used to connect the nodes in general. For this present work, we are assuming the direct connected path distance between any two points are identical and of length 100m for simplification.

Propagation Delay of copper wire: The understanding of signal propagation delay in copper media is essential. Electrical signals through copper wires travel at approximately 2/3 times the speed of light in vacuum. This is the propagation speed of the signal through the

copper. As we are aware of that an Ethernet operates at a speed of 10,000,000 bits per second or 10Mbps, we can find out that the length of wire which is occupied by a single bit is approximately equal to 20 meters.

Speed of light in a vacuum = $3 \times 10^8 = 300,000,000$ meters/ second

Speed of electricity in a copper cable = $(2/3) \times 300,000,000$ meters/ second=200,000,000 meters/ second

Length required for a single bit $\Rightarrow (200,000,000\text{ms}) / (10,000,000 \text{ bits/s}) = 20 \text{ meter/bit}$

The delay for a single bit in copper wire is $= \frac{20 \text{ meter/bit}}{200,000,000 \text{ meters/ second}} = 10^{-7} \text{ second/bit} = 100\text{ns/bit}$

So, from the above calculation, to travel 20m for a single bit requires 100ns.

Relying upon these delays, a table for different path lengths including processing delay of node is given in Table-3. Assuming a node delay is 24ns for classical CMOS. While calculating the path delay we are to involve all the nodes in a path. Hence a path having length 1 contains 2 node, having length 2 contains 3nodes and so forth. So the delay of a path of two nodes is $24 \times 2 + 100 = 148\text{ns}$. In the same way, all the possible delays for different path lengths of 1, 2, 3, 4, 5 and 6 for a 2^6 node-network drawn in Fig. 6 are presented in Table-3 below. As the maximum delay is 768ns, so in the worst case, the speed of the network will be $f = \frac{1}{768\text{ns/bit}} = 0.001302 \times 10^9 \text{ bit/sec} = 1.302\text{Mb/sec}$.

Table-3

Sl. No	Input node	Output node	Routing path	Path length	Delays (ns)
1	16	20	16→20	1	148
2	9	33	9→1→33	2	272
3	24	36	24→20→4→36	3	396
4	15	51	15→11→3→19→51	4	520
5	16	46	16→20→22→30→14→46	5	644
6	42	21	42→43→41→45→37→53→21	6	768

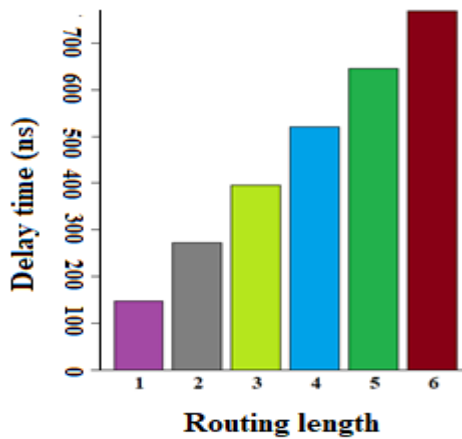


Fig.6 Delay time vs. routing path length

II. Conclusion

In the present work, we are concentrated in making a network having 2^n nodes in general. For the space limitation, the value of $n=6$ is chosen. And accordingly, we are concentrated in 64 nodes. Among these 64 nodes, any pair of separate two nodes at any time can be selected for data/packet transferring. These data/packet would reach the destination point without any trouble as we have investigated that in any column for the table-1, no two node points (of six bits) are identical. If the two such identical node points would have stayed in any column, there would have a collision or deadlock. For creating a proper sequence of nodes, a circuit is implemented that can provide the required nodes whenever a pair of input points (source, destination) are set to. A 8×8 grid is created to show the distinct communication paths using arrow lines. The memory size utilized for manipulating the nodes in a routing path is at most 10.94%. Time delays for different possible path lengths are calculated. Time complexity is proportional to the depth of the tree i.e. $O(l)$. Speed through the network will be 1.302Mb/sec.

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